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Metric trees, hyperconvex hulls and extensions. (English summary)

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Summary: “In this paper we examine the relationship between hyperconvex hulls and metric trees. After providing a linking construction for hyperconvex spaces, we show that the four-point property is inherited by the hyperconvex hull, which leads to the theorem that every complete metric tree is hyperconvex. We also consider some extension theorems for these spaces.”

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Note: This list reflects references listed in the original paper as accurately as possible with no attempt to correct errors.